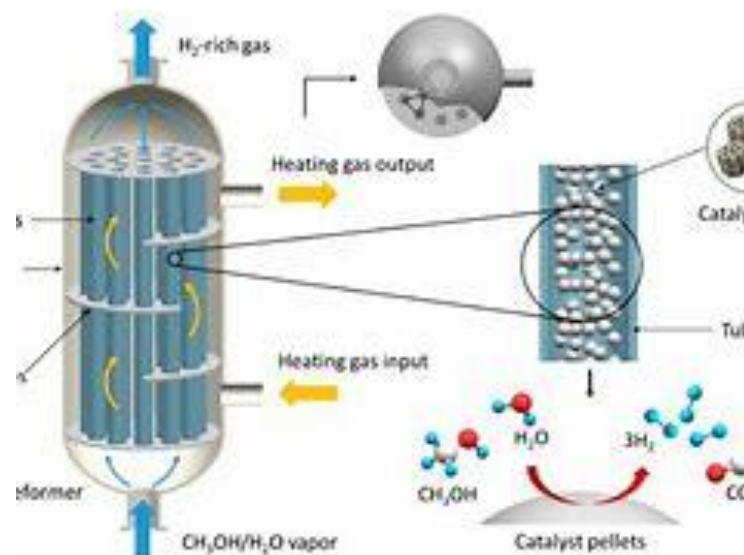
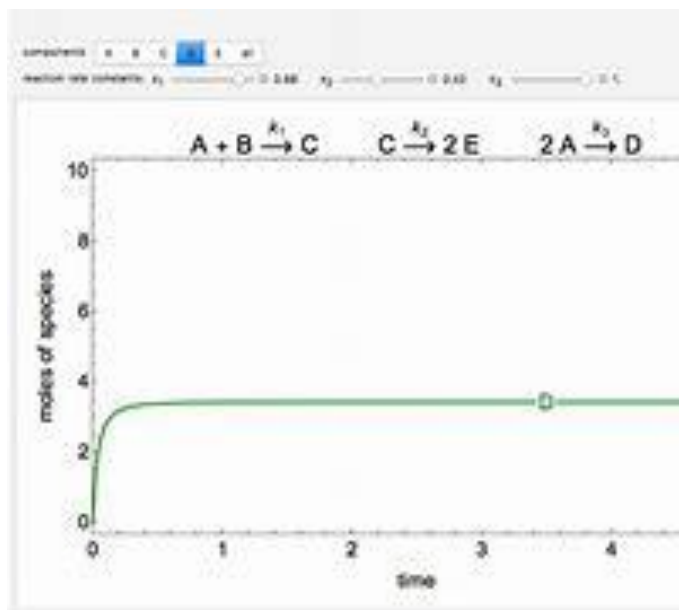


# Reactor Design II



Week 4

## Multiple Reactions and Semibatch Reactor

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# Introduction

- Chemical Reaction Engineering (CRE) involves the study of reaction rates, mechanisms, and reactor design.
- This lecture focuses on the role of semibatch reactors in maximizing selectivity and optimizing reaction conditions.

# Topics to be Addressed

- - Fundamentals of Semibatch Reactors
- - Mole Balances and Stoichiometry
- - Rate Laws and Reversible Reactions
- - Numerical Analysis using Polymath
- - Practical Examples and Case Studies

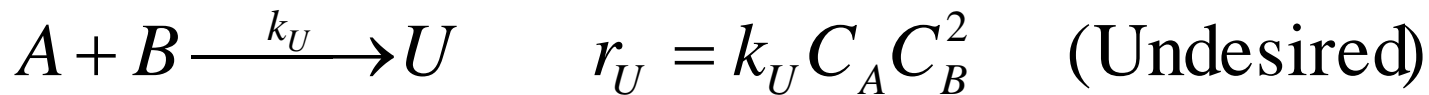
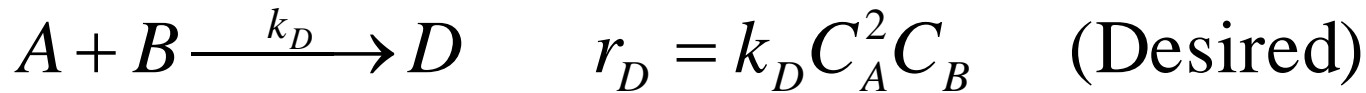
# Objectives

- By the end of this lecture, students will be able to:
- - Understand the operational principles of semibatch reactors.
- - Apply mole balances, rate laws, and stoichiometry to reactor design.
- - Analyze reversible reactions in semibatch reactors.
- - Utilize numerical methods for reactor analysis.

# Introduction

- Semibatch reactors are highly effective for controlling reaction dynamics, especially in liquid-phase reactions where selectivity is crucial.
- This session explores theoretical foundations, practical applications, and numerical approaches using Polymath for analysis.

# Selectivity in Multiple Reactions



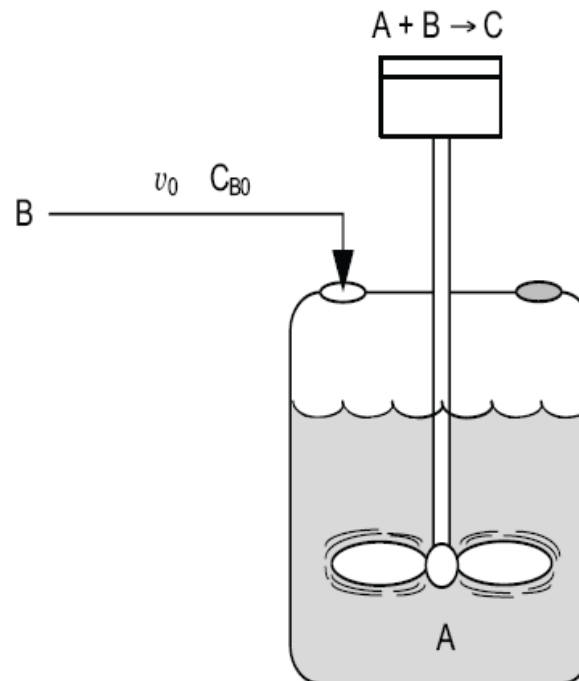
	Selectivity	Yield
Instantaneous	$S_{D/U} = r_D / r_U$	$Y_D = r_D / -r_A$
Overall	$\hat{S}_{D/U} = F_D / F_U$	$\hat{Y}_D = F_D / (F_{A0} - F_A)$

$$S_{D/U} = \frac{r_D}{r_U} = \frac{k_D C_A^2 C_B}{k_U C_A C_B^2} = \frac{k_D C_A}{k_U C_B}$$

Keep  $C_A$  high and  $C_B$  low.

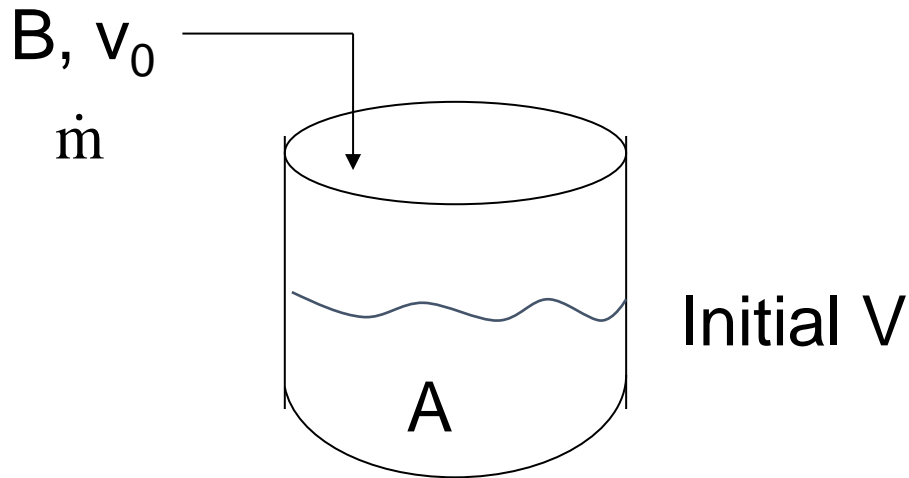
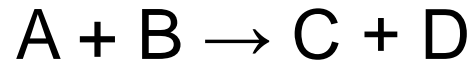
# Semibatch Reactors

- Semibatch reactors can be very effective in maximizing selectivity in liquid phase reactions.
- The reactant that starts in the reactor is always the limiting reagent



# Semibatch Reactors

## Semibatch reactors



Liquid level and volume increase



# Semibatch Reactors

**1) Mass Balance:**  $\frac{dm}{dt} = \dot{m}$

$$\dot{m} = \nu_0 \rho_0 \quad \text{and} \quad m = V \rho_0$$

$$\frac{dm}{dt} = \rho_0 \frac{dV}{dt} = \rho_0 \nu_0$$

$$\frac{dV}{dt} = \nu_0$$

$$t = 0 \quad V = V_0 \quad V = V_0 + \nu_0 t$$

# Semibatch Reactors

## 1) Mole Balance on Species A:

$$[\text{in}] - [\text{out}] + [\text{gen}] = [\text{acc}]$$

$$0 - 0 + r_A V = \frac{dN_A}{dt}$$

$$\frac{dN_A}{dt} = \frac{d[C_A V]}{dt} = V \frac{dC_A}{dt} + C_A \frac{dV}{dt}$$

$$\frac{dV}{dt} = v_0$$

$$\frac{dC_A}{dt} = r_A - \frac{v_0 C_A}{V}$$

# Semibatch Reactors

## 1) Mole Balance on Species B:

$$F_{B0} - 0 + r_B V = \frac{dN_B}{dt}$$

$$\frac{dN_B}{dt} = \frac{d[C_B V]}{dt} = V \frac{dC_B}{dt} + C_B \frac{dV}{dt}$$

$$F_{B0} = C_{B0} \nu_0 \quad \frac{dV}{dt} = \nu_0$$

$$\frac{dC_B}{dt} = r_B + \frac{(C_{B0} - C_B) \nu_0}{V}$$

# Semibatch Reactors

## 1) Mass and Mole Balance Summary

$$(1) \quad \frac{dC_A}{dt} = r_A - \frac{\nu_0 C_A}{V}$$

$$(2) \quad \frac{dC_B}{dt} = r_B - \frac{\nu_0 (C_{B0} - C_B)}{V}$$

$$(3) \quad \frac{dC_C}{dt} = r_C - \frac{\nu_0 C_C}{V}$$

$$(4) \quad \frac{dC_D}{dt} = r_D - \frac{\nu_0 C_D}{V}$$

$$(5) \quad V = V_0 + \nu_0 t$$

# Semibatch Reactors

## 2) Rate Laws

$$(6) \quad r_A = kC_A C_B$$

## 3) Stoichiometry

$$\frac{-r_A}{1} = \frac{-r_B}{1} = \frac{r_C}{1} = \frac{r_D}{1}$$

$$(7) \quad r_B = r_A$$

$$(8) \quad r_C = -r_A$$

## 4) Parameters

$$C_{A0}, V_0, \nu_0, k, C_{B0}$$

$$(9) \quad r_D = -r_A$$

$$(10) \quad X = \frac{N_{A0} - N_A}{N_{A0}}$$

$$(11) \quad N_{A0} = C_{A0} V_0$$

$$(12) \quad N_A = C_A V$$

# Semibatch Reactors



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## POLYMATH Report Ordinary Differential Equations

### Calculated values of DEQ variables

	Variable	Initial value	Minimal value	Maximal value	Final value
1	Ca	0.05	7.731E-06	0.05	7.731E-06
2	Cao	0.05	0.05	0.05	0.05
3	Cb	0	0	0.0125077	0.0125077
4	Cbo	0.025	0.025	0.025	0.025
5	Cc	0	0	0.0121468	0.0083256
6	Cd	0	0	0.0121468	0.0083256
7	k	2.2	2.2	2.2	2.2
8	ra	0	-0.0001644	0	-2.127E-07
9	rate	0	0	0.0001644	2.127E-07
10	t	0	0	500.	500.
11	V	5.	5.	30.	30.
12	vo	0.05	0.05	0.05	0.05
13	Vo	5.	5.	5.	5.
14	X	0	0	0.9990722	0.9990722

### Differential equations

- $d(Ca)/d(t) = ra - vo * Ca / V$
- $d(Cb)/d(t) = ra + (Cbo - Cb) * vo / V$
- $d(Cc)/d(t) = -ra - vo * Cc / V$
- $d(Cd)/d(t) = -ra - vo * Cd / V$

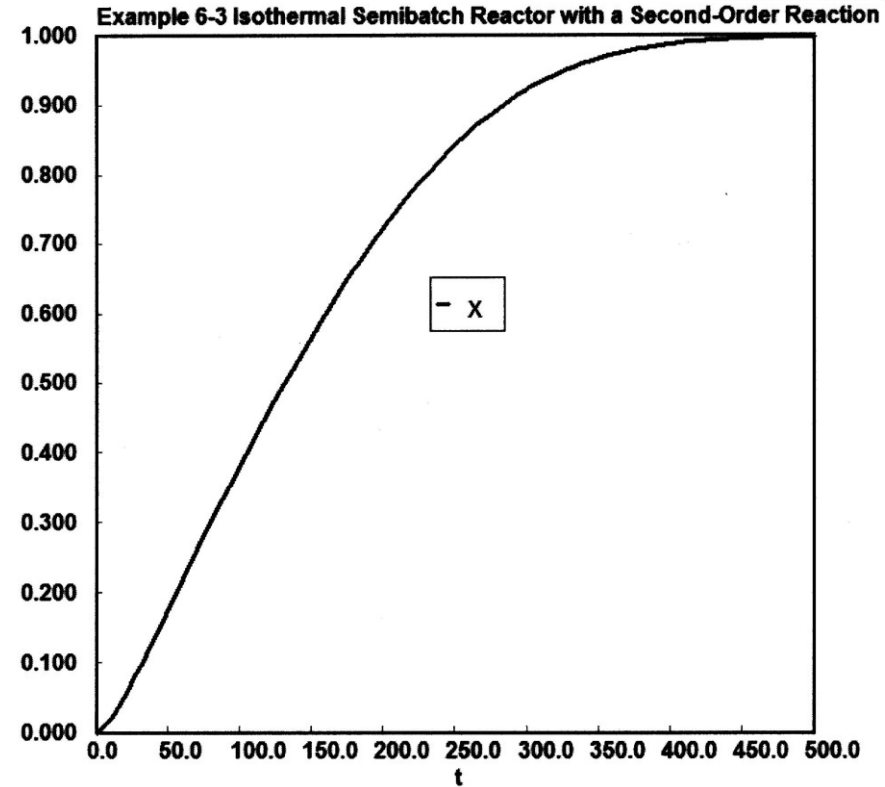
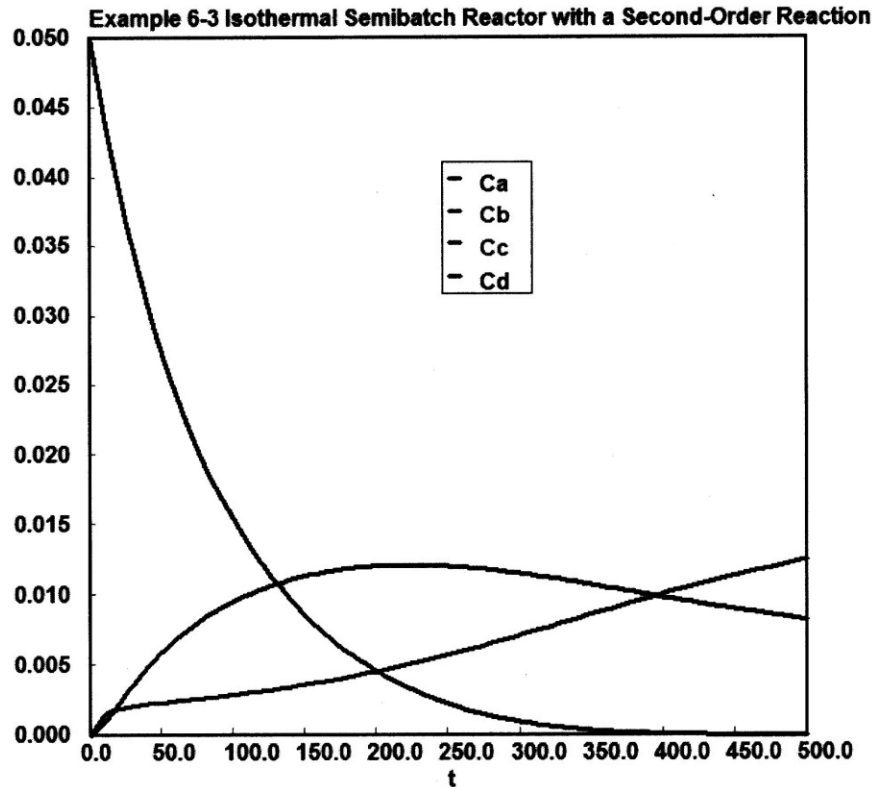
### Explicit equations

- $vo = 0.05$
- $Vo = 5$
- $V = Vo + vo * t$
- $k = 2.2$
- $Cbo = 0.025$
- $ra = -k * Ca * Cb$
- $Cao = 0.05$
- $rate = -ra$
- $X = (Cao * Vo - Ca * V) / (Cao * Vo)$

# Semibatch Reactors

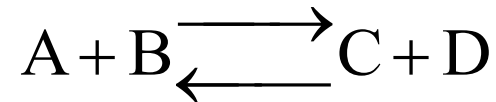


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# Equilibrium Conversion in Semibatch Reactors with Reversible Reactions

Consider the following reaction:



Everything is the same as for the irreversible case, except for the rate law:

$$-r_A = k_A \left[ C_A C_B - \frac{C_C C_D}{K_C} \right]$$



# Equilibrium Conversion in Semibatch Reactors with Reversible Reactions

Where:

$$C_A = \frac{N_{A0}(1-X)}{V}$$

$$C_B = \frac{(F_{B0}t - N_{A0}X)}{V}$$

$$C_C = C_D = \frac{N_{A0}X}{V}$$

At equilibrium,  $-r_A = 0$  then

$$K_C = \frac{C_{Ce}C_{De}}{C_{Ae}C_{Be}} = \frac{N_{Ce}N_{De}}{N_{Ae}N_{Be}} = \frac{N_{A0}X_e^2}{(1-X_e)(F_{B0}t - N_{A0}X_e)}$$

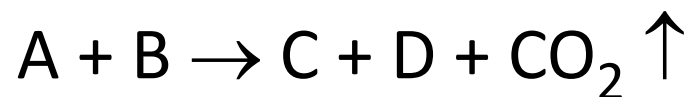
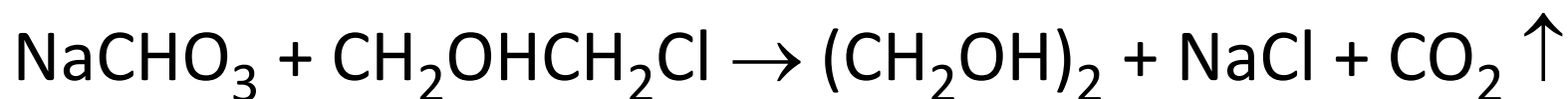
$X_e$  changes with time.

# Example 1: Semibatch Reactors



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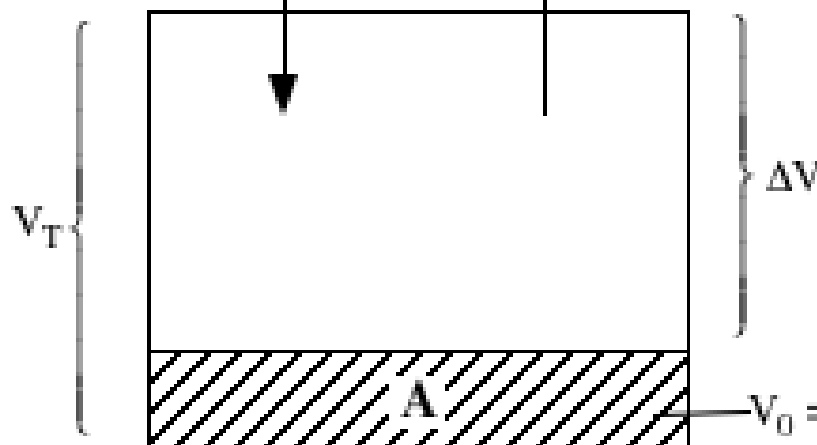
Sodium Bicarbonate + Ethylene Chlorohydrin  $\rightarrow$  Ethylene Glycol + NaCl +  $\text{CO}_2 \uparrow$



$$F_{B0} = 0.1 \frac{\text{mol}}{\text{min}}$$

$$C_{B0} = 1.5 \text{ M}$$

B  $\rightarrow$   $\text{CO}_2$



$$k = 5.1 \frac{\text{dm}^3}{\text{mol} \cdot \text{h}}$$

$$V_0 = 1500 \text{ dm}^3 \text{ with } C_{A0} = 0.75 \text{ M}$$

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## Semibatch Reactors in terms of Moles



### Mole Balances

$$A \quad (1) \quad \frac{dN_a}{dt} = r_A V$$

$$B \quad (2) \quad \frac{dN_b}{dt} = F_{B0} + r_B V$$

$$C \quad (3) \quad \frac{dN_c}{dt} = r_C V$$

$$D \quad (4) \quad N_D = N_C$$

$$CO_2 \quad 0 = -F_{CO_2} + r_{CO_2} V$$

$$(5) \quad F_{CO_2} = r_{CO_2} V$$

$$-r_A = -r_B = r_C = r_D = r_{CO_2}$$

$$(6) \quad \frac{dV}{dt} = v_0 - v_{CO_2}$$

$$(7) \quad v_{CO_2} = \frac{F_{CO_2} MW_{CO_2}}{RHO}$$

$$(8) \quad MW = 44$$

$$(9) \quad RHO = 1000$$

$$(10) \quad C_a = N_A / V$$

$$(11) \quad C_B = N_B / V$$

$$(12) \quad r_A = -k C_A C_B$$

$$(13) \quad X = \frac{N_{a0} - N_a}{N_{a0}}$$

$$(14) \quad N_{a0} = V_0 C_{a0}$$

## Rate Laws

Rest of the Polymath Statements  
Similar to Concentration Program

# Semibatch: Moles, $N_a$ , $N_b$ , etc.

## POLYMATH Report

Ordinary Differential Equations

### Calculated values of DEQ variables

	Variable	Initial value	Minimal value	Maximal value	Final value
1	Ca	0.75	8.845E-14	0.75	8.845E-14
2	Cao	0.75	0.75	0.75	0.75
3	Cb	0	0	0.15303	0.15303
4	Cbo	1.5	1.5	1.5	1.5
5	Cc	0	0	0.4967829	0.45909
6	Cd	0	0	0.4967829	0.45909
7	Fbo	6.	6.	6.	6.
8	FCO2	0	0	5.987114	1.692E-10
9	k	5.1	5.1	5.1	5.1
10	MWCO2	44.	44.	44.	44.
11	Na	1125.	2.167E-10	1125.	2.167E-10
12	Nao	1125.	1125.	1125.	1125.
13	Nb	0	0	375.	375.
14	Nc	0	0	1125.	1125.
15	ra	0	-0.0039389	0	-6.903E-14
16	rho	1000.	1000.	1000.	1000.
17	t	0	0	250.	250.
18	V	1500.	1500.	2450.5	2450.5
19	vCO2	0	0	0.263433	7.443E-12
20	vo	4.	4.	4.	4.
21	X	0	0	1.	1.

### Differential equations

$$1 \quad d(V)/d(t) = v_o - v_{CO2}$$

$$2 \quad d(N_c)/d(t) = -r_a * V$$

$$3 \quad d(N_b)/d(t) = F_{bo} + r_a * V$$

$$4 \quad d(N_a)/d(t) = r_a * V$$

### Explicit equations

$$1 \quad C_{bo} = 1.5$$

$$2 \quad F_{bo} = 6$$

$$3 \quad C_{ao} = 0.75$$

$$4 \quad C_c = N_c / V$$

$$5 \quad N_{ao} = 1125$$

$$6 \quad X = (N_{ao} - N_a) / N_{ao}$$

$$7 \quad k = 5.1$$

$$8 \quad \rho = 1000$$

$$9 \quad MW_{CO2} = 44$$

$$10 \quad C_a = N_a / V$$

$$11 \quad C_b = N_b / V$$

$$12 \quad r_a = -k * C_a * C_b$$

$$13 \quad v_o = F_{bo} / C_{bo}$$

$$14 \quad F_{CO2} = -r_a * V$$

$$15 \quad v_{CO2} = F_{CO2} * MW_{CO2} / \rho$$

$$16 \quad C_d = C_c$$

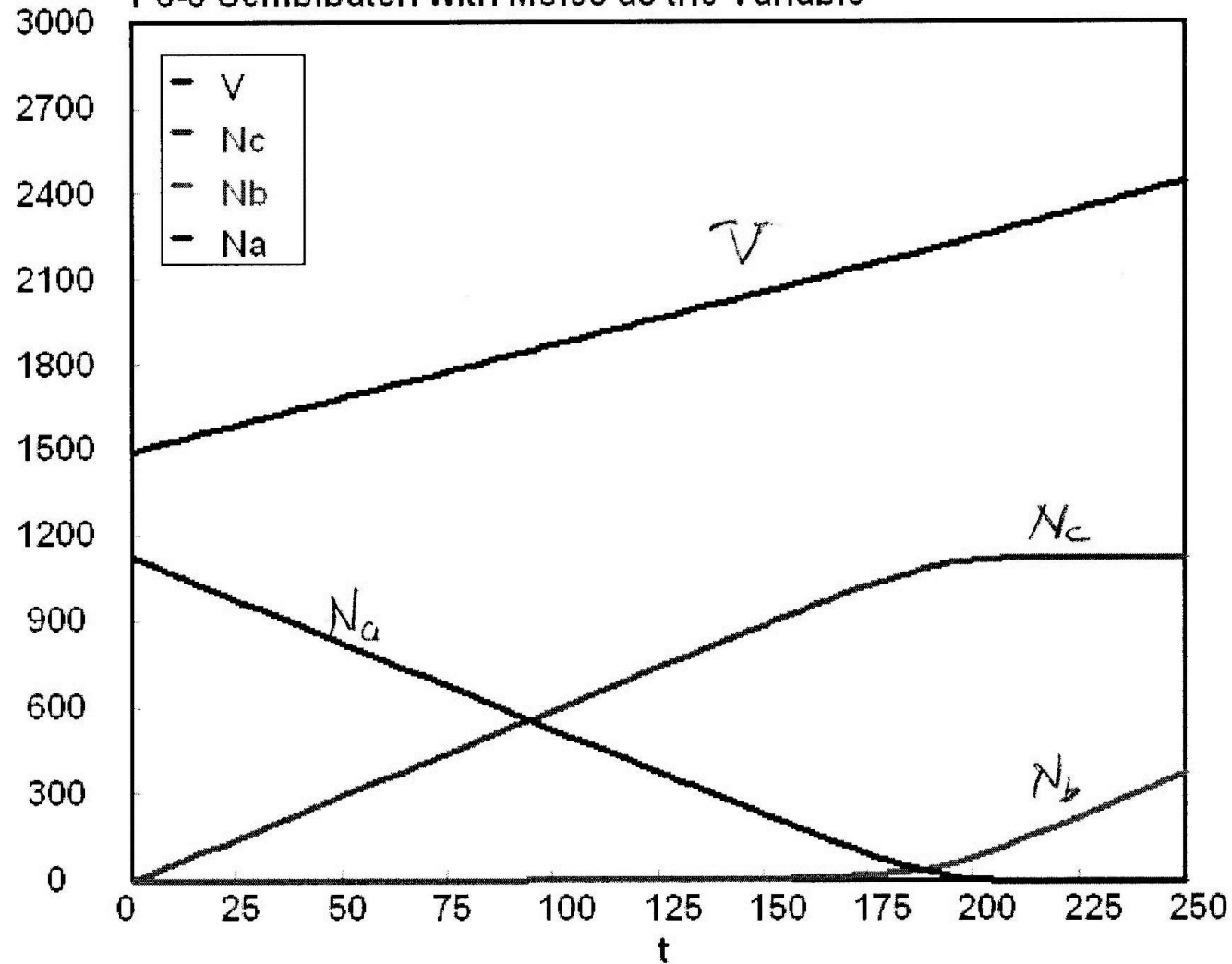


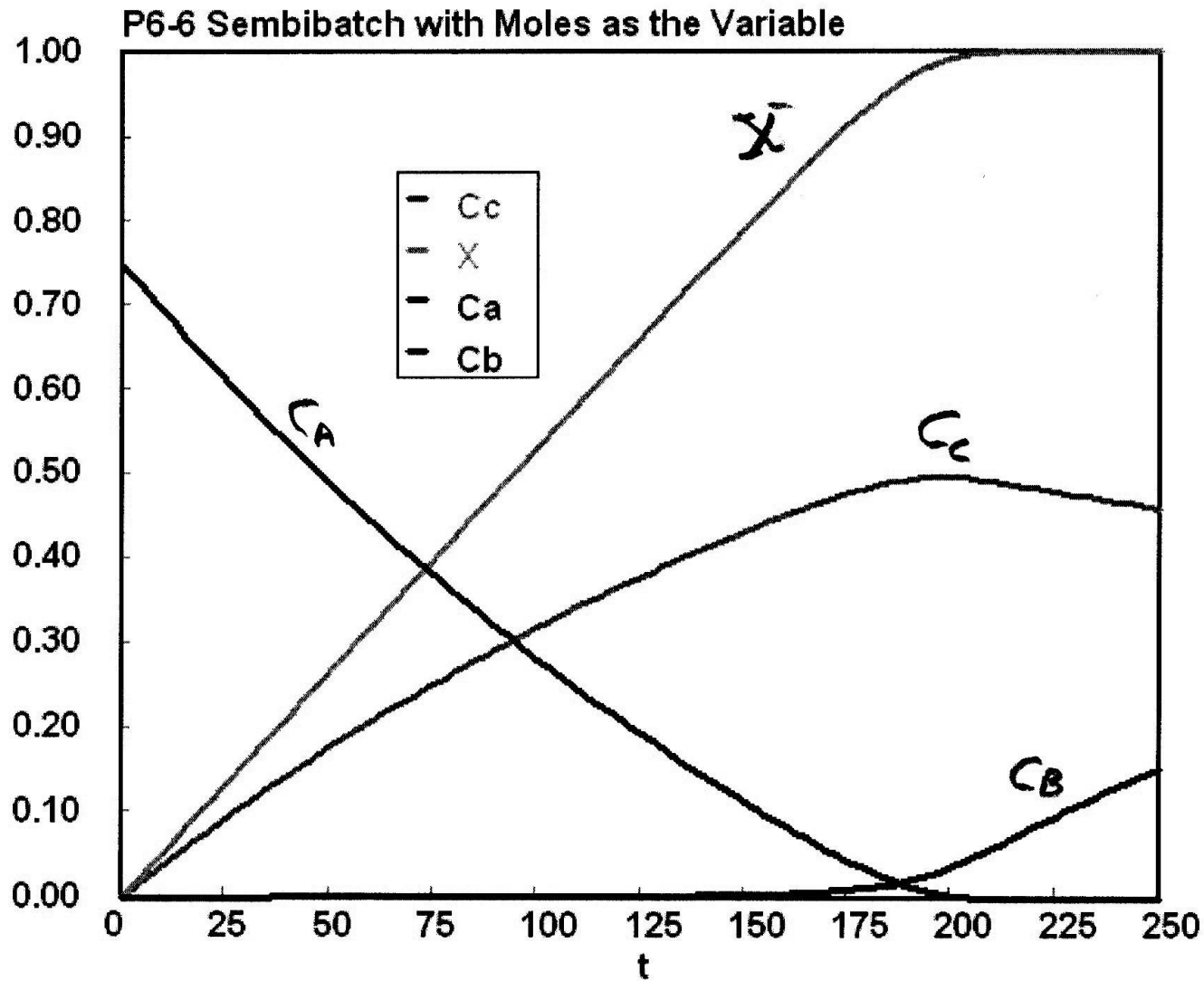
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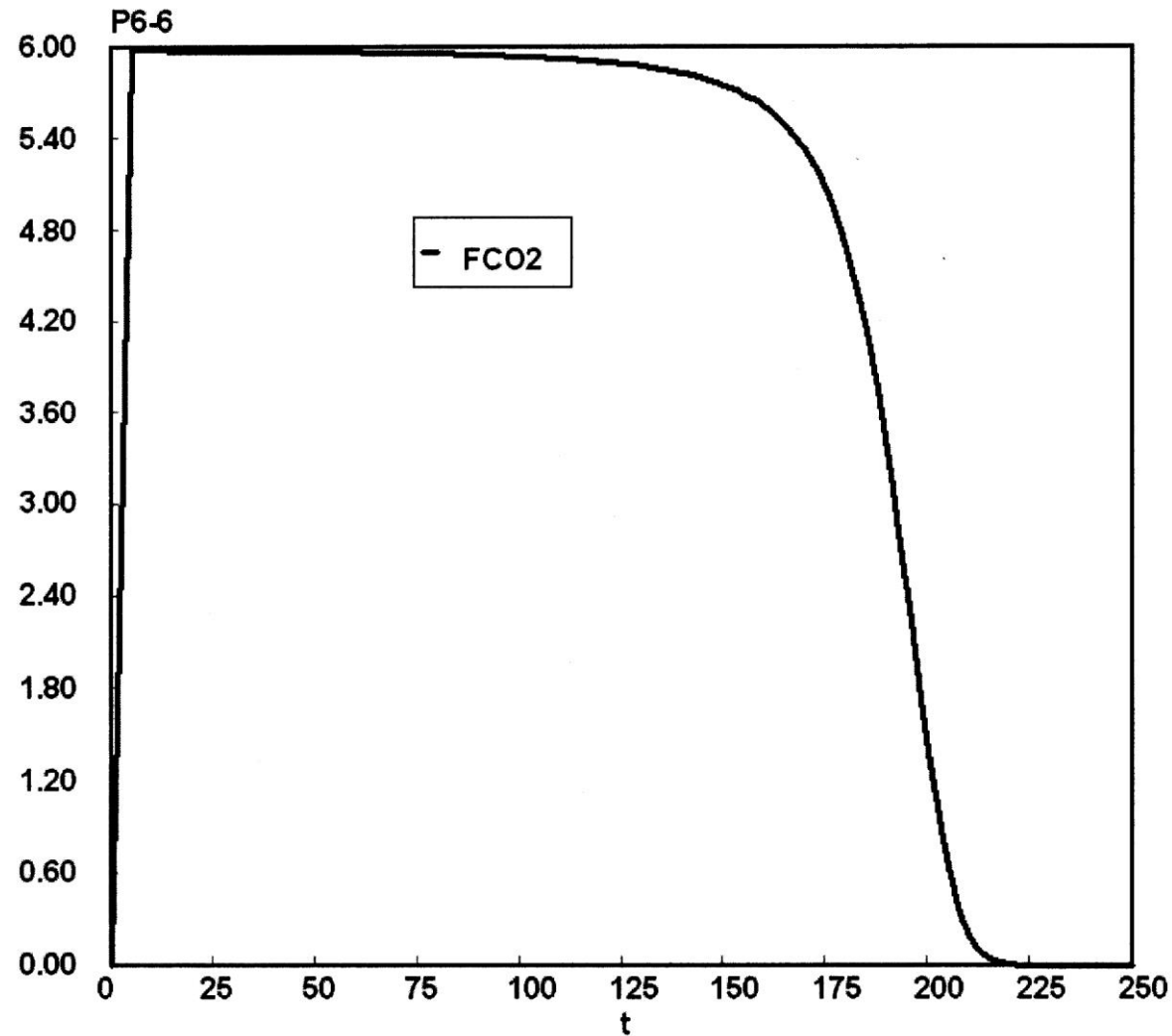
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P6-6 Sembibatch with Moles as the Variable











# P6-6 Semibatch: Concentrations $C_A$ , $C_B$ , $C_C$

## POLYMATH Report

Ordinary Differential Equations

### Calculated values of DEQ variables

	Variable	Initial value	Minimal value	Maximal value	Final value
1	Ca	0.75	8.846E-14	0.75	8.846E-14
2	Cao	0.75	0.75	0.75	0.75
3	Cb	0	0	0.15303	0.15303
4	Cbo	1.5	1.5	1.5	1.5
5	Cc	0	0	0.496826	0.45909
6	CC	0	0	0.496827	0.45909
7	Cd	0	0	0.496827	0.45909
8	Fbo	6.	6.	6.	6.
9	FCO2	0	0	5.987132	1.692E-10
10	k	5.1	5.1	5.1	5.1
11	MWCO2	44.	44.	44.	44.
12	Na	1125.	2.168E-10	1125.	2.168E-10
13	Nao	1125.	1125.	1125.	1125.
14	NC	0	0	1125.	1125.
15	Nc	0	0	1125.	1125.
16	ra	0	-0.0039413	0	-6.904E-14
17	rate	0	0	0.0039413	6.904E-14
18	rho	1000.	1000.	1000.	1000.
19	t	0	0	250.	250.
20	V	1500.	1500.	2450.5	2450.5
21	vCO2	0	0	0.2634338	7.444E-12
22	vo	4.	4.	4.	4.
23	Vo	1500.	1500.	1500.	1500.
24	X	0	0	1.	1.

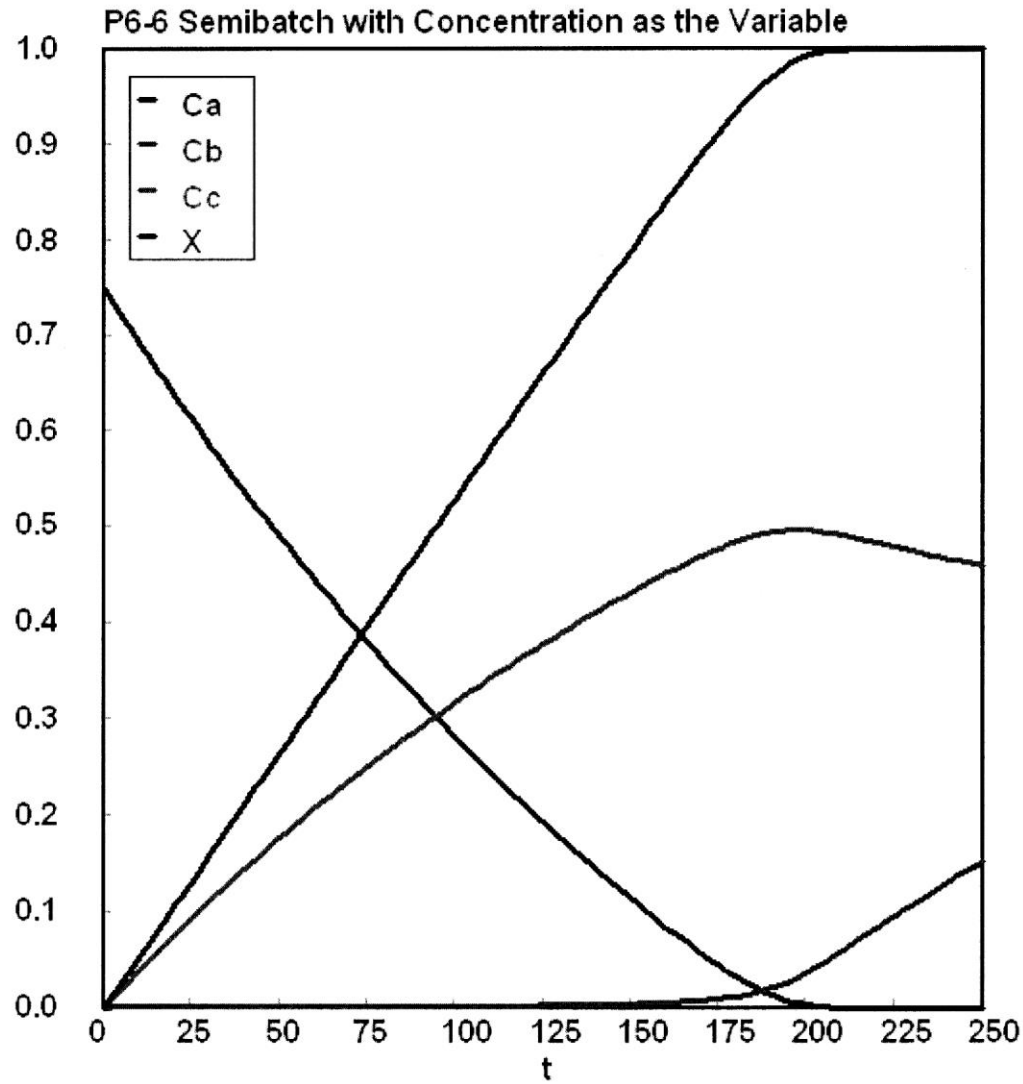
### Differential equations

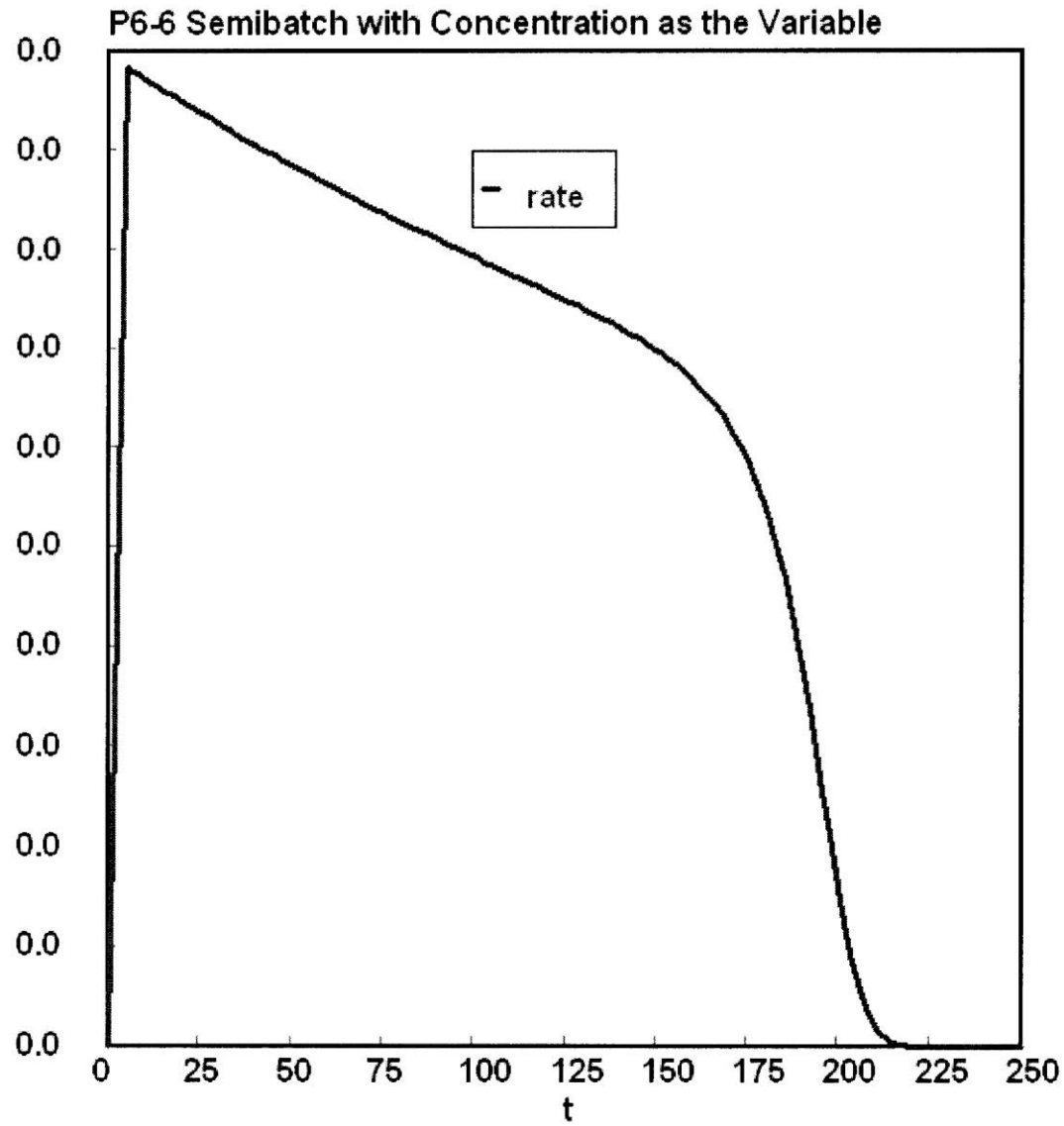
- $d(Ca)/d(t) = ra + ((vo-vCO2) / V) * (-Ca)$
- $d(Cb)/d(t) = ra + vo*Cbo/V + ((vo-vCO2) / V) * (-Cb)$
- $d(Cc)/d(t) = -ra + ((vo-vCO2) / V) * (-Cc)$
- $d(V)/d(t) = vo-vCO2$

### Explicit equations

- $Cd = Cc$
- $Fbo = 6$
- $Cao = 0.75$
- $Vo = 1500$
- $Na = Ca*V$
- $k = 5.1$
- $ra = -k * Ca * Cb$
- $Nao = Cao*Vo$
- $rate = -ra$
- $rho = 1000$   
 $rho=1000g \text{ per } dm^3$
- $MWCO2 = 44$
- $FCO2 = -ra*V$
- $NC = Nao - Na$
- $Cbo = 1.5$
- $vo = Fbo / Cbo$
- $vCO2 = MWCO2*FCO2/rho$
- $CC = NC/V$
- $Nc = Cc * V$
- $X = 1 - Ca * V / (Cao*Vo)$







# Semibatch Reactors



Three Forms of the **Mole Balances** applied to **Semibatch Reactors**:

1. Molar Basis  $\frac{dN_A}{dt} = r_A V$

$$\frac{dN_B}{dt} = F_{B0} + r_B V$$

2. Concentration Basis  $\frac{dC_A}{dt} = r_A - C_A \frac{\nu_0}{V}$   $\frac{dN_A}{dt} = r_A V$

$$\frac{dC_B}{dt} = r_B + (C_{B0} - C_B) \frac{\nu_0}{V} \quad \frac{dN_B}{dt} = F_{B0} + r_B V$$

3. Conversion  $\frac{dX}{dt} = \frac{-r_A V}{N_{A0}}$

# Semibatch Reactors



Consider the following elementary reaction:



$$-r_A = kC_A C_B$$

The combined **Mole Balance**, **Rate Law**, and **Stoichiometry** may be written in terms of number of moles, conversion, and/or concentration:

<u>Conversion</u>	<u>Concentration</u>	<u>No. of Moles</u>
$\frac{dX}{dt} = \frac{k(1-X)(N_{B0} + F_{B0}t - N_{A0}X)}{V_0 + v_0t}$	$\frac{dC_A}{dt} = r_A - C_A \frac{v_0}{V}$	$\frac{dN_A}{dt} = r_A V$
	$\frac{dC_B}{dt} = r_A + (C_{B0} - C_B) \frac{v_0}{V}$	$\frac{dN_B}{dt} = F_{A0} + r_B V$



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# Polymath Equations

<u>Conversion</u>	<u>Concentration</u>	<u>Moles</u>
$d(X)/d(t) = -r_a * V / N_{ao}$	$d(C_a)/d(t) = r_a - (C_a * v_o)/V$	$d(N_a)/d(t) = r_a * V$
$r_a = -k * C_a * C_b$	$d(C_b)/d(t) = r_b + ((C_{bo} - C_b) * v_o)/V$	$d(N_b)/d(t) = r_b * V + F_{bo}$
$C_a = N_{ao} * (1 - X) / V$	$r_a = -k * C_a * C_b$	$r_a = -k * C_a * C_b$
$C_b = (N_{bi} + F_{bo} * t - N_{ao} * X) / V$	$r_b = r_a$	$r_b = r_a$
$V = V_o + v_o * t$	$V = V_o + v_o * t$	$V = V_o + v_o * t$
$V_o = 100$	$V_o = 100$	$V_o = 100$
$v_o = 2$	$v_o = 2$	$v_o = 2$
$N_{ao} = 100$	$F_{bo} = 5$	$F_{bo} = 5$
$F_{bo} = 5$	$N_{ao} = 100$	$C_a = N_a / V$
$N_{bi} = 0$	$C_{bo} = F_{bo} / v_o$	$C_b = N_b / V$
$k = 0.1$	$k = 0.01$	$k = 0.01$
	$N_a = C_a * V$	
	$X = (N_{ao} - N_a) / N_{ao}$	



# Are you ready?



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# Summary

- In this lecture, we discussed:
  - - The unique features and applications of semibatch reactors.
  - - How to maximize selectivity in multiple reactions.
  - - Key concepts: mole balances, rate laws, and stoichiometry.
  - - Numerical approaches for analyzing semibatch reactor performance.
- Semibatch reactors are versatile tools in chemical engineering, enabling precise control over reaction dynamics for optimized outcomes.